

Logic Programming, Prolog

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Overview

- Logic programming
- Formal logic
- Prolog

Logic Programming

- To express programs in a form of symbolic logic, and use a logic inferencing process to produce results
 - Symbolic logic is the study of symbolic abstractions that capture the formal features of logical inference
- Logic programs are declarative

Formal Logic

 A proposition is a logical statement or query about the state of the "universe"

- It consists of objects and the relationship between objects

 Formal logic was developed to describe propositions, with the goal of allowing those formally stated propositions to be checked for validity

Symbolic Logic

- Symbolic logic can be used for three basic needs of formal logic
 - To express propositions,
 - To express the relationship between propositions, and
 - To describe how new propositions can be inferred from other propositions that are assumed to be true

Formal logic & mathematics

- Most of mathematics can be thought of in terms of logic
- The fundamental axioms of number and set theory are the initial set of propositions, which are assumed to be true
- **Theorems** are the additional propositions that can be inferred from the initial set

First-Order Predicate Calculus

- The particular form of symbolic logic that is used for logic programming is called first-order predicate calculus
- It contains propositions and clausal form

Propositions

- The objects in propositions are represented by simple terms
 - Simple terms can be either constants or variables
 - A constant is a symbol that represents an object
 - A variable is a symbol that can represent different objects at different times

Propositions

- The simplest propositions, which are called atomic propositions, consist of compound terms
- A compound term represents mathematical relation. It contains
 - a functor: the function symbol that names the relation, and
 - an ordered list of parameters

Compound Terms

- A compound term with a single parameter is a I-tuple
 - E.g. man(jake)
- A compound term with two parameters is a 2-tuple
 - E.g., like(bob, steak)

Compound Terms

- All of the simple terms in the propositions, such as man, jake, like, bob, and steak, are constants
- They mean whatever we want them to mean
 - E.g., like(bob, steak) may mean
 - o Bob likes steak, or
 - o steak likes Bob, or
 - o Bob is in some way similar to a steak, or
 - Does Bob like steak?

Propositions can also contain variables, such as man(X)

Compound Propositions

 Atomic propositions can be connected by logical connectors

<u>Name</u>	<u>Symbol</u>	<u>Example</u>	<u>Meaning</u>
negation	_	¬a	not a
conjunction	\cap	$\mathbf{a} \cap \mathbf{b}$	a and b
disjunction	\cup	$a \cup b$	a or b
equivalence	≡	$a \equiv b$	a is equivalent to b
implication	\supset	$a \supset b$	a implies b b implies a
	\subseteq	$a \subset b$	b implies a

Compound Propositions (cont'd)

Quantifiers—used to bind variables in propositions

- Universal quantifier: \forall
 - $\forall x.P means$ "for all x, P is true"
- Existential quantifier: \exists

 $\exists x.P - means$ "there exists a value of x such that P is true"

– Examples

 $\bigcirc \forall x.(manager(x) \supset employee(x))$

 $\bigcirc \exists x.(mother(mary,x) \cap male(x))$

First-Order Predicate Calculus

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Clausal Form

- **Clausal form** is a standard form of propositions
- It can be used to simplify computation by an automated system

Clausal Form

• A proposition in clausal form has the following general syntax:

 $\frac{BI \cup B2 \cup ... \cup Bn}{consequent} \subset \frac{AI \cap A2 \cap ... \cap Am}{antecedent}$

- Consequent is the consequence of the truth of the antecedent
- Meaning

- If all of the A's are true, then at least one B is true

Examples

- likes(bob, mcintosh) ⊂ likes(bob, apple) ∩ apple(mcintosh)
- father(john, alvin) ∪ father(john, alice) ⊂ father(alvin, bob) ∩ mother(alice, bob) ∩ grandfather(john, bob)

Predicate Calculus

- Predicate calculus describes collections of propositions
- Resolution is the process of inferring propositions from given propositions
- Resolution can detect any inconsistency in a given set of proposition

An Exemplar Resolution

• If we know:

 $older(terry, jon) \subset mother(terry, jon)$ wiser(terry, jon) $\subset older(terry, jon)$

 We can infer the proposition: wiser(terry, jon) ⊂ mother(terry, jon)

Horn Clauses

- When propositions are used for resolution, only
 Horn clauses can be used
 - A proposition with zero or one term in the consequent is called a Horn clause
 - If there is only one term in the consequence, the clause is called a Headed Horn clause
 - \circ E.g., person(jake) \subset man(jake)
 - For stating Inference Rules in Prolog
 - If there is no term in the consequence, the clause is called a Headless Horn clause
 - E.g., man(jake)
 - For stating **Facts and Queries** in Prolog

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Logic Programming Languages

- Logical programming languages are declarative languages
- Declarative semantics: It is simple to determine the meaning of each statement, and it does not depend on how the statement might be used to solve a problem
 - E.g., the meaning of a proposition can be concisely determined from the statement itself

Logic Programming Languages (cont'd)

- Logical Programming Languages are **nonprocedural**
- Instead of specifying how a result is computed, we describe the desired result and let the computer figure out how to compute it

An Example

E.g., sort a list

sort(new_list, old_list) \subset permute(old_list, new_list) \cap sorted(new_list)

sorted(list) $\subset \forall j$ such that $I \leq j \leq n$, list(j-1) \leq list(j)

where permute is a predicate that returns true if its second parameter is a permutation of the first one

Key Points about Logic Programming

- Nonprocedural programming sounds like the mere production of concise software requirements specifications
 - It is a fair assessment
- Unfortunately, logic programs that use only resolution face the problems of execution efficiency

Key Points about Logic Programming

- The best form of a logic language has not been determined
- Good methods of creating programs in logic programming languages have not yet been developed