

198:415 Spring 1999
 Professor Barbara G. Ryder
 Quiz on Grammars
 2/15/99

The following grammar describes two binary operations on strings, % and \$. % is concatenation; “abc” % “def” evaluates to “abcdef”. \$ reverses its first operand and then concatenates it onto the end of its second operand. “abc” \$ “def” evaluates to “defcba”.

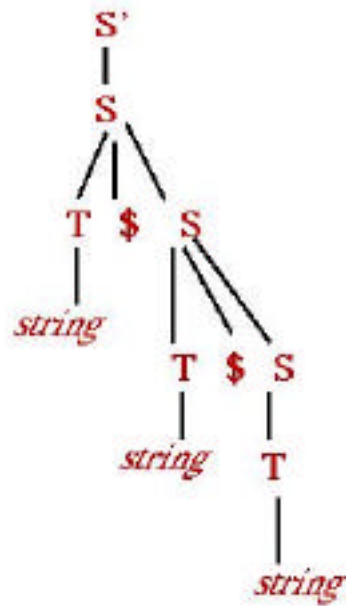
\$ has higher precedence than %.

S' S
 S T \$ S | T % S | T
 T *string* (where *string* tokens are alphabetic symbols surrounded by double quotes.)

- a. What is the value of the following expression:
 “xyz” \$ “hij” % “abc” ? **hijzyxabc**
- b. Show a rightmost derivation of the sentence “a” % “b” % “c”.

S' S T % S T % T % S T % T % T
 T % T % *string* T % *string* % *string*
string % *string* % *string*

- c. Show the parse tree for the sentence “a” \$ “b” \$ “c”.



- d. Change the grammar so that it is clear from the structure of the grammar that \$ has higher precedence than %. Make sure your changed grammar generates the same strings as the original grammar does.

S' S
S E % S | E
E T \$ E | T
T *string* (where *string* tokens are alphabetic symbols surrounded by double quotes.)

- e. Is \$ left associative or right associative? **Right associative**