## CS4204 Computer Graphics Fall 2007 Homework Assignment 2

Assignment 2 is due on Tuesday, 10/03/2007 3:30pm. You need to turn your homework in before midterm start. Please write clearly on paper.
Note: There are 10 points for each question.

Q1. Viewport transform is a 2D transformation that maps normalized device coordinate system on to window coordinate system. What is the 2D transformation matrix for the following OpenGL command?
glViewport( 20, 30, width/3, height*1.5 );

Q2. Please explain when windows reshape callback event happens. And display callback event?

Q3. What is the 2D transformation matrix for rotate 60 degree around point ( $-1,2$ ) ?

Q4. For scan conversion for lines, we have Bresenham (midpoint) algorithm.
(a). What is implicit function $F(x, y)$ of a line?
(b) Given the following figure. If our current choice is $\mathrm{P}\left(\mathrm{p}_{\mathrm{x}}, \mathrm{p}_{\mathrm{y}}\right)$, how can we choose the next point $\mathrm{P}^{\prime}\left(\mathrm{p}_{\mathrm{x}+1}, \mathrm{p}_{\mathrm{y}}\right)$.


Q5. Let's represent 2D translation as $\operatorname{TR}(x, y)$, rotation as $R(\theta)$, scale as $S\left(s_{x}, s_{y}\right)$. Please write down the series of transformations produces the reflection of a two dimensional point about an arbitrary line $y=3 x+5$ ?

Consider the following three coordinate systems ( $\mathrm{O}, \mathrm{A}, \mathrm{B}$ ) for questions 6-10:


Notation: $\boldsymbol{M}_{\boldsymbol{s T}}$ is a $3 \times 3$ homogeneous matrix that transforms points from coordinate system $\boldsymbol{S}$ to coordinate system $\boldsymbol{T}$.

Q6. What are the coordinates of $P$ in coordinate system $\boldsymbol{O}$ ?

Q7. What are the coordinates of P in coordinate system $\boldsymbol{A}$ ?

Q8. What are the coordinates of P in coordinate system $\boldsymbol{B}$ ?

Q9. Express $\boldsymbol{M}_{\boldsymbol{O B}}$ in terms of $\boldsymbol{M}_{\boldsymbol{A O}}$ and $\boldsymbol{M}_{\boldsymbol{B} \boldsymbol{A}}$.

Q10. Given a vector $\mathbf{a}$ and a plane with normal vector $\mathbf{n}$, what is the angle between $\mathbf{a}$ and the projection of $\mathbf{a}$ on the plane?

Q11. What is the difference between orthographical projection and perspective projection?

Q12. Please draw the diagram for OpenGL transformation pipeline.

