CS 6824:

Deep Generative Learning for Molecular Synthesis

Acknowledgement:

Many of the images in the slides are derived from images.google.com or other publicly available sources.

Recurrent neural network



$$\boldsymbol{y}_i = f_o\left(\boldsymbol{h}_i\right)$$

- Standard RNN suffers from vanishing gradient problem
- RNN variants of long short-term memory (LSTM) and gated recurrent unit (GRU) aim to address that

RNN-based generative models with TL

- RNN generative model for *de novo* molecular generation using stacked LSTM layer
- LSTM-based RNN model combined with a sampling temperature, which rescales the probability distribution of output sequences

RNN-based generative models with RL

• **REINVENT**

- RNN-based generative model for molecular *de novo* design through augmented episodic likelihood-based RL
- Policy-based RL to fine-tune an RNN-based agent for generating molecules with given desirable properties



RNN-based generative models with RL

- **ReLeaSE**
 - Combines the two deep neural networks (generative model G and predictive model P trained separately
 - G is a stack-augmented RNN (Stack-RNN) architecture to learn hidden rules of forming sequences of letters for generating valid SMILES molecules
 - P is analogous to a Quantitative Structure-Activity Relationship (QSAR) model for molecular properties prediction with only taking SMILES string as an input vector. It is based on a deep neural network consisting of embedding layer, LSTM layer and two dense layers



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Autoencoders

How can we learn this latent space? Train the model to use these features to **reconstruct the original data**



• Autoencoding = Automatically encoding data

Traditional autoencoders



• Deterministic encoding

Variational autoencoders (VAEs)



 Replace the deterministic bottleneck layer with a stochastic sampling operation

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Variational autoencoders (VAEs)



- Going from learning a vector of latent variables to a vector of means and variances which describe the prob. distribution associated with each of the latent variables
- Both encoder and decoder are probabilistic in nature

VAE for molecular data



$$\text{ELBO}\left(\boldsymbol{\phi}, \boldsymbol{\theta}\right) = \mathbb{E}_{q_{\boldsymbol{\phi}}(\boldsymbol{z}|\boldsymbol{x})} \left[\log p_{\boldsymbol{\theta}}\left(\boldsymbol{x}|\boldsymbol{z}\right)\right] - \text{KL}\left(q_{\boldsymbol{\phi}}\left(\boldsymbol{z}|\boldsymbol{x}\right)||p\left(\boldsymbol{z}\right)\right)$$

- **Encoder**: learning to represent molecules in a continuous manner that facilitates the prediction and optimization of their properties
- **Decoder**: learning to map an optimized continuous representation back into a molecular with improved properties

RNN- and AE-based generative models

- ChemVAE
 - Encoder converts the discrete representations of molecules (SMILES strings in this case) into real-valued fix-dimensional continuous vectors
 - Decoder transforms the vectors to SMILES strings
 - Adds Gaussian noise to the encoder with penalty term guaranteeing the valid decoding
 - A predictive model based on multilayer perceptron, was joined into VAE to predict the molecular properties from latent space



RNN- and AE-based generative models

• Grammar VAE

- Utilizes a context-free grammar (CFG) to form a parse tree, which is decomposed into a sequence of production rules defined as 4-tuple G = (V, T, R, S), containing a finite set of nonterminal symbols V, a finite set of terminal symbols T, a finite set of production rules R, and a distinct start symbol S.
- The SMILES strings can be generated via adopting production rules recursively (sampling from start symbol till no nonterminals left)
- Rules are fed into an encoder with convolutional neural network architecture, then an RNN architecture as a decoder for generating syntactically valid SMILES
- Decoder transforms the vectors into SMILES strings



Generative adversarial network



- A generative model G, which learns a map from a prior to the data distribution to sample new data points,
- discriminative model D, which learns to classify whether samples come from the real data distribution rather than from G
- Those two models are implemented as deep neural networks and trained alternatively with stochastic gradient descent. G and D have different objectives, and they can be seen as two players in a minmax game

$$\min_{G} \max_{D} V(D, G) = \mathbb{E}_{\boldsymbol{x} \sim p_{data}(\boldsymbol{x})} \left[\log D(\boldsymbol{x}) \right] + \mathbb{E}_{\boldsymbol{z} \sim p_{\boldsymbol{z}}(\boldsymbol{z})} \left[\log \left(1 - D(G(\boldsymbol{z})) \right) \right]$$

• G tries to generate samples to fool the discriminator and D tries to differentiate samples correctly

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RNN & GAN-based generative models with RL

- Objective reinforced GAN (ORGAN)
 - GAN architecture is combined with reward functions with RL to generate SMILES strings
 - ^o G_θ is a LSTM-based generator parameterized by θ, that produces high-quality sequences X1:T = (x1, ..., xT). And a discriminator D_φ parameterized by φ is a convolutional neural network specifically for sequence classification
 - $\circ~G_{\theta}$ is trained as an agent and the reward function R was supplied by $D\varphi~$ to fool $D\varphi$
 - $\circ~D_\varphi$ is trained to classify real and generated SMILES sequences



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RNN & GAN-based generative models with RL

• Reinforced adversarial neural computer

- \circ generator G_{θ} is a differentiable neural computer (DNC), which is is an LSTM controller with external
- memory (like Stack-RNN) and its advantages lay in its powerful memory to reconstruct and generate complex and much longer SMILES strings than LSTM
- The action value function of candidate states (partial sequences) was calculated by Monte Carlo search.



Graph-based generative models



 Given an example of chemical molecule, a 2D structure is a graph with nodes as its atoms and edges between two nodes as its bonds

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Recurrent graph-based generative models

• GraphNet

- Uses the structure of molecular graph to create representations of atoms and bonds via an information propagation process (GRU); these representations are used to make sequential graph building decisions
- Probabilistic decision-making modules (parameterized by training with known molecular graphs)
 - adding a new node or not (with probabilities provided by a *f*_{addnode} module)
 - adding a new edge or not (probabilities provided by *f*_{addedge} module)
 - picking one node to connect to the new node with typed edges (probabilities provided by *f_{nodes}* module)



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Recurrent graph-based generative models

• MolMP

- While GraphNet uses GRU to obtain atomic representations, which are integrated to molecular representation by Gated Sum,MolMP uses Graph Convolutional Network (GCN) and average pooling for atomic and molecular representations
- The actions of *f*_{addnode}, *f*_{addedge} and *f*_{nodes} are merged into a single *f*_{append} step, and *f*_{connect} is used to avoid the repeated operation of adding edges. It helps to reduce the number of steps during generation.adding a new node or not



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VAE-based generative models

• GraphVAE

- A molecular graph can be characterized by G = (A, E,F) with its adjacency matrix A, edge attribute tensor E, and node attribute tensor F
- VAE was used to jointly train an encoder $q_{\phi}(z|G)$ and a decoder $p_{\theta}(G|z)$ to map between the space of graphs G and the continuous embedding $z \in \mathbb{R}^{D}$, where ϕ and θ are learned parameters. A regularization term, KL-divergence, is added into the latent code space with a prior isotropic Gaussian distribution p(z) = N(0, I), which is aimed to approximate the two distributions of $q\phi(z|G)$ and p(z).



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VAE & RNN-based generative models

• NeVAE

- A step-wise generative model for undirected molecular graphs based on VAEs.
- Defines a probabilistic encoding for each atom by extracting atomic information from K different layers
- This information is fed into a neural network to make the product obey the stand normal distribution for each atom
- This atom-based embedding strategy is invariant to permutations of the atoms and do not depend on the number of atoms and bonds, thus allowing for variable-sized molecular graphs
- A whole molecular graph is decoded out with dynamic recurrent updating of the edges and edge weight



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Adversarial autoencoder



- Inspired by VAE and GAN, AAE is proposed as a standard AE regularized by an adversarial learning (AL) procedure rather than a KL divergence penalty
- While the KL regularization in VAE is usually used to impose a prior distribution on the latent code *z*, the AL regularization in AAE is utilized to match the posterior distribution to a prior distribution
- While the posterior distribution in VAE is usually a Gaussian distribution with mean and variance predicted by the encoder, posterior distribution in AAE is encouraged to match a prior arbitrary distribution
- G tries to fool the discriminator D by mimicking the prior arbitrary distribution

